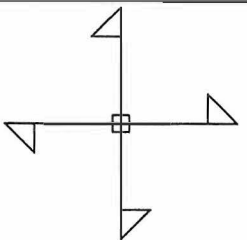


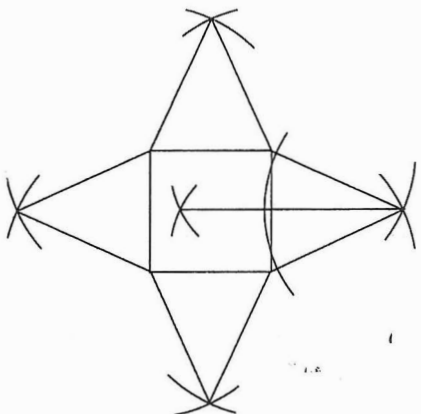
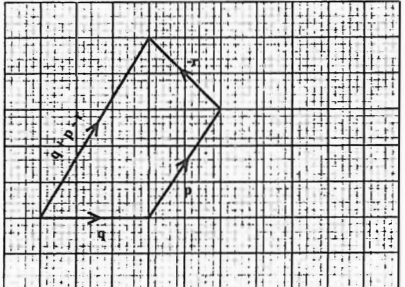
KALA MATH PP1 2024 MARKING SCHEME

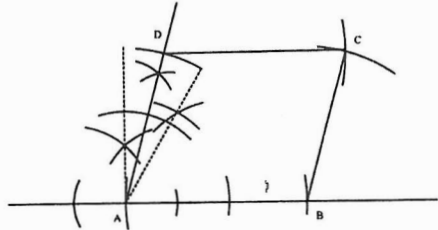
No	Marking Scheme	Marks	Comments																
1.	Numerator $\frac{14}{5} \text{ of } \frac{25}{21} \div \frac{3}{14} - \frac{1}{4}$ $\frac{10}{3} \times \frac{14}{3} - \frac{1}{4}$ $= \frac{551}{36}$	M1																	
	Denominator $\frac{23}{8} + \frac{13}{8}$ $= \frac{36}{8}$ $\frac{551}{36} \div \frac{36}{8}$ $= 3 \frac{65}{162}$			M1															
		A1																	
		3																	
2.	$\frac{80}{100} \times 5500 \times 201.15 \times 0.95$ $= 840807$ $840807 - 772204.5 = 68602.5$ $= \frac{6860215}{152.45}$ $= 450 \text{ US dollars}$	M1																	
		M1																	
		A1																	
		3																	
3.	<table border="1" style="display: inline-table; border-collapse: collapse;"> <tr><td>3</td><td>243</td><td>270</td><td>324</td></tr> <tr><td>3</td><td>81</td><td>90</td><td>108</td></tr> <tr><td>3</td><td>27</td><td>30</td><td>36</td></tr> <tr><td></td><td>9</td><td>10</td><td>12</td></tr> </table> $GCD = 3 \times 3 \times 3 = 27$	3	243	270	324	3	81	90	108	3	27	30	36		9	10	12	M1	
	3	243	270	324															
3	81	90	108																
3	27	30	36																
	9	10	12																

No	Marking Scheme	Marks	Comments
	$\text{Total number of pieces} = \frac{243}{27} + \frac{270}{27} + \frac{324}{27}$ $= 9 + 10 + 12$ $= 31$	M1  A1 3	
4.		B1	
		B1	
		3	
5.	$1.3 \text{ rad} = 74.48^\circ$ $\frac{285.52}{360} \times 2 \times \frac{22}{7} \times 10.5 + 10.5 + 10.5$ $= 73.35 \text{ cm}$	M1 M1 A1 3	
		M1	
		A1	
		3	
6.	$\cos 3x = -\frac{1}{2}$ $3x = \cos^{-1}(-0.5) = 120^\circ$ $3x = 120$ $x = 40^\circ$ $3x = 240$ $x = 80^\circ$ $3x = 480$ $x = 160^\circ$ $x = 40^\circ, 80^\circ \text{ or } 160^\circ$	M1 M1  A1  B1 4	
		M1	
		A1	
		B1	
7.	$2^{6x+6} - 2^{6x-2} = 255$ $2^{6x} \times 2^6 - \frac{2^{6x}}{2^2} = 255$	M1	

No	Marking Scheme	Marks	Comments
	$2^{6x} \left(64 - \frac{1}{4}\right) = 255$ $2^{6x} \left(\frac{255}{4}\right) = 255$ $2^{6x} = 2^2$ $6x = 2$ $x = \frac{1}{3}$	M1  A1 3	
8.	$300 = \frac{1}{2} \times 15 \times x + 5 \times x + \frac{1}{2}(x + 1.5x)5 + \frac{1}{2} \times 15 \times 1.5x$ $300 = 7.5x + 5x + 6.25x + 11.25x$ $30x = 300$ $x = 10$ $1.5x = 1.5 \times 10$ $= 15 \text{ m/s}$	M1  M1 A1 3	
9.	$\frac{2x^2 - 5xy - 2y^2}{y(5xy + 12y^2 - 2x^2)}$ $\frac{2x^2 - 8yx + 3yx - 12y^2}{y[2x(x - 4y) + 3y(x - 4y)]}$ $\frac{(2x + 3y)(x - 4y)}{y[(3y + 2x)(4y - x)]}$ $= -\frac{1}{y}$	M1  M1 A1 3	
10.	$12x = 180^\circ$ $x = 15^\circ$ $\angle OCB = 60^\circ$	M1 A1 B1 3	

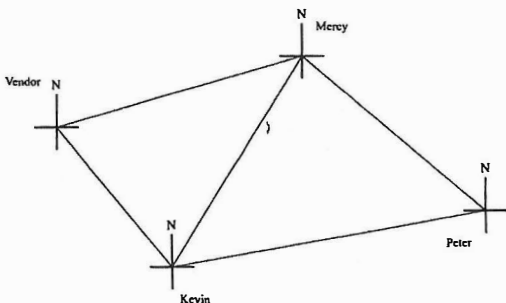
No	Marking Scheme	Marks	Comments
11.	$155 + 104 + (n - 2)143 = (2n - 4)90$ $259 + 143n - 286 = 180n - 360$ $-37n = -333$ $n = 9 \text{ sides}$	M1  M1 A1 3	
12.	$\frac{5}{3} - 2x < 1 - \frac{2}{3}x$ $\frac{2}{3} < \frac{4}{3}x$ $2 < 4x$ $\frac{1}{2} < x$ $1 - \frac{2}{3}x \leq 2 - x$ $\frac{x}{3} \leq 1$ $x \leq 3$ $\frac{1}{2} < x \leq 3$ Range 0, 1, 2, 3	M1  M1 A1 3	

No	Marking Scheme	Marks	Comments	
13.	(a)		B1	
			B1	
		B1	4	
		B1		
	(b) Height = 5.4 cm ± 0.1			
14.		B1		
		B1		
		2		

No	Marking Scheme	Marks	Comments
15.	74 cm, 35.6 cm, 52.4 cm 72 cm, 32.6 cm, 50.4 cm $\frac{72}{12} = 6$ $\frac{33.0}{8.4} = 4$ $\frac{50.4}{8.4} = 6$ Total = 6 × 4 × 6 = 144	M1	
		M1	
		A1	
		3	
16.	 Length AC = 10.4 cm ± 0.1	B1	
		B1	
		B1	
		B1	
		4	

SECTION II (50 Marks)

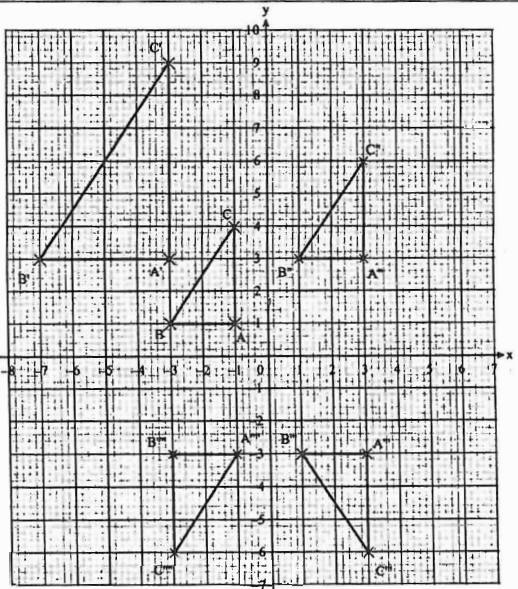
No	Marking Scheme	Marks	Comments
17.	<p>(a) <math>3y = -4x + 12</math></p> $y = -\frac{4}{3}x + 4$ $m_1 = m_2 = -\frac{4}{3}$ $\frac{y - 4}{x + 7} = -\frac{4}{3}$ $3y = -4x - 16$ $y = -\frac{4x}{3} - \frac{16}{3}$ <p>Coordinates of y- intercept</p> $(0, -5\frac{1}{3})$ <p>(b) <math>m_1 \times m_2 = -1</math></p> $m_2 = \frac{3}{4}$ $\frac{y + 7}{x + 5} = \frac{3}{4}$ $3x + 15 = 4y + 28$ $3x - 4y = 13$ <p>(c) <math>4x + 3y = -16</math></p> $3x - 4y = 13$ $12x + 9y = -48$ $12x - 16y = 52$ $25y = -100$ $y = -4$ $3x - 4(-4) = 13$ $x = -1$ $(-1, -4)$	<p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	
		10	

No	Marking Scheme	Marks	Comments																					
18.	<p>a)</p>  <p>b) (i) <math>321^\circ \pm 1</math></p> <p>(ii) <math>N32^\circ E \pm</math></p> <p>(iii) <math>7.8 \text{ cm} \pm 0.1</math></p> $7.8 \times 10 = 78 \text{ km}$ <p>(iv) <math>80 + 75 + 100 + 78</math></p> $= 333 \text{ km}$	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>10</p>																						
19.	<p>a)</p> <table border="1" data-bbox="1444 1093 1780 1348"> <thead> <tr> <th>x</th> <th>f</th> <th>fx</th> </tr> </thead> <tbody> <tr> <td>34</td> <td>2</td> <td>68</td> </tr> <tr> <td>39</td> <td>8</td> <td>312</td> </tr> <tr> <td>44</td> <td>10</td> <td>440</td> </tr> <tr> <td>49</td> <td>6</td> <td>294</td> </tr> <tr> <td>54</td> <td>4</td> <td>216</td> </tr> <tr> <td></td> <td><math>\Sigma f = 30</math></td> <td><math>\Sigma fx = 1330</math></td> </tr> </tbody> </table>	x	f	fx	34	2	68	39	8	312	44	10	440	49	6	294	54	4	216		$\Sigma f = 30$	$\Sigma fx = 1330$	<p>B1</p> <p>B1</p>	
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	$\bar{x} = \frac{\sum fx}{\sum f}$ $= \frac{1330}{30}$ $= 44.33$ $= 44$	M1 A1																									
	b) (i) <table border="1" style="margin-left: 20px;"> <thead> <tr> <th>Class</th> <th>Tally</th> <th>f</th> <th>cf</th> </tr> </thead> <tbody> <tr> <td>32 - 36</td> <td>//</td> <td>2</td> <td>2</td> </tr> <tr> <td>37 - 41</td> <td>/// //</td> <td>8</td> <td>10</td> </tr> <tr> <td>42 - 46</td> <td>/// ///</td> <td>10</td> <td>20</td> </tr> <tr> <td>47 - 51</td> <td>/// /</td> <td>6</td> <td>26</td> </tr> <tr> <td>52 - 56</td> <td>////</td> <td>4</td> <td>30</td> </tr> </tbody> </table>	Class	Tally	f	cf	32 - 36	//	2	2	37 - 41	/// //	8	10	42 - 46	/// ///	10	20	47 - 51	/// /	6	26	52 - 56	////	4	30	B1 B1 B1	
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47 - 51	/// /	6	26																								
52 - 56	////	4	30																								
	(ii) $Median\ age = 41.5 + \frac{(15-10)5}{10}$ $= 41.5 + 2.5$ $= 43.5$	M1 M1 A1 10																									
20.	a) (i) $\frac{3500000}{x}$ (ii) $\frac{3500000}{x+30}$ b) $\frac{3500000}{x} - \frac{3500000}{x+30} = 26500$ $26500x^2 + 78500x - 105000000 = 0$ $7x^2 + 210x - 28000 = 0$ $x = \frac{-210 \pm \sqrt{210^2 - 4 \times 7 \times -28000}}{2 \times 7}$ $= \frac{-210 \pm 910}{14}$ $= 50$	B1 B1 M1 M1 M1 A1 M1 A1																									

No	Marking Scheme	Marks	Comments
	c) $\frac{3500000}{5} = 70000$ $= 3500000 - 300000$ $\frac{3200000}{80} = 40000$ $40000 : 70000$ $4 : 7$	M1 A1 10	
21.	(i) $\frac{x+20}{x} = \frac{6}{4}$ $4x + 80 = 6x$ $2x = 80$ $x = 40$ $Height = 40 + 20$ $= 60$ (ii). $Vol = \left(\frac{1}{3} \times 12 \times 18 \times 60\right) - \left(\frac{1}{3} \times 12 \times 8 \times 40\right)$ $4320 - 1280$ $= 3040$ (iii) $\sqrt{9^2 + 60^2} = 60.71$ $\sqrt{6^2 + 40^2} = 40.45$ $\sqrt{6^2 + 60^2} = 60.30$ $\sqrt{4^2 + 40^2} = 40.20$ $\left(\frac{1}{2} \times 12 \times 60.71\right) - \left(\frac{1}{2} \times 8 \times 40.45\right)$ $202.46 \times 2 = 402.92$	M1 M1 A1 M1M1 A1 B1 M1	

No	Marking Scheme	Marks	Comments
	$\left(\frac{1}{2} \times 18 \times 60.30\right) - \left(\frac{1}{2} \times 12 \times 40.20\right)$ $301.5 \times 2 = 603$ $402.92 + 603 + 8 \times 12 + 12 \times 18$ $= 1317.92$	M1 A1 10	
22.	<p>(a) (i) <math>12 + \frac{24}{2}</math>  <math>= 24 \text{ cm}^2</math></p> <p>(ii) <math>24 \text{ cm}^2 = 10 \text{ km}^2</math>  <math>1 \text{ cm}^2 = 416666.67 \text{ m}^2</math>  <math>1 : 645.49</math></p> <p>(b) (i) <math>A = \frac{1}{2}(7.25 + 11.25) + 2(1.25 + 2.75 + 4.75 + 5.25 + 6)</math>  <math>= 49.25</math></p> <p>(ii) <math>\text{Area} = 1(4 + 1 + 4 + 5 + 6 + 9)</math>  <math>= 29</math></p>	B1 M1 A1	

No	Marking Scheme	Marks	Comments
23.	 <p>a) <math>A(-1, 1)</math> <math>B(-3, 1)</math> <math>C(-1, 4)</math></p>	B1 B1 B1  B1 B1 B1  B1 B1 B1  10	
24.	<p>(a) (i) <math>2x^2 + 4xh = 1425</math>  <math>4xh = 1425 - 2x^2</math>  <math>h = \frac{1425 - 2x^2}{4x}</math></p> <p>(ii) <math>V = x^2h</math>  <math>V = \frac{1425x^2 - 2x^4}{4x}</math>  <math>V = \frac{1425x - 2x^3}{4}</math></p> <p>(b) (i) At maximum <math>\frac{dV}{dx} = 0</math>  <math>\frac{dV}{dx} = \frac{1425}{4} - \frac{6x^2}{4}</math></p>	M1 M1 A1  B1  M1 M1	

No	Marking Scheme	Marks	Comments
	$\frac{1425}{4} - \frac{6x^2}{4} = 0$ $x = 15.4$ <p>(ii)</p> $V = \frac{1425x - 2x^3}{4}$ $V = \frac{1425(15.4) - 2(15.4)^3}{4}$ $= 5367.67$	M1 A1   M1 A1 <b>10</b>	